

# HARDY WEINBERG THEOREM DERIVATION

In a population with two alleles “A” and “a”...

Let proportion of AA = D (dominant genotype);

Aa = H (heterozygote genotype)

aa = R (recessive genotype)

Then  $D + H + R = 1$

Let p = allele frequency of “A” & q = allele freq. of “a”

$p = D + \frac{1}{2} H$ ;  $q = R + \frac{1}{2} H$

m		f	Freq. mating	AA	Progeny Aa	aa
AA	x	AA	DD	$D^2$		
AA	x	Aa	DH	$DH/2$	$DH/2$	
Aa	x	AA	HD	$DH/2$	$DH/2$	
AA	x	aa	DR		DR	
aa	x	AA	RD		DR	
Aa	x	Aa	HH	$H^2/4$	$H^2/2$	$H^2/4$
aa	x	Aa	RH		$HR/2$	$HR/2$
Aa	x	aa	HR		$HR/2$	$HR/2$
aa	x	aa	RR			$R^2$

$$\begin{aligned} \text{Totals: } & D^2 + DH + 1/4 H^2 \\ & = (D + 1/2 H)^2 \\ & = p^2 \end{aligned}$$

$$\begin{aligned} & DH + 2 DR + HR + H^2/2 \\ & = 2 (D + 1/2 H) (1/2 H + R) \\ & = 2pq \end{aligned}$$

$$\begin{aligned} & 1/4 H^2 + HR + R^2 \\ & = (1/2 H + R)^2 \\ & = q^2 \end{aligned}$$